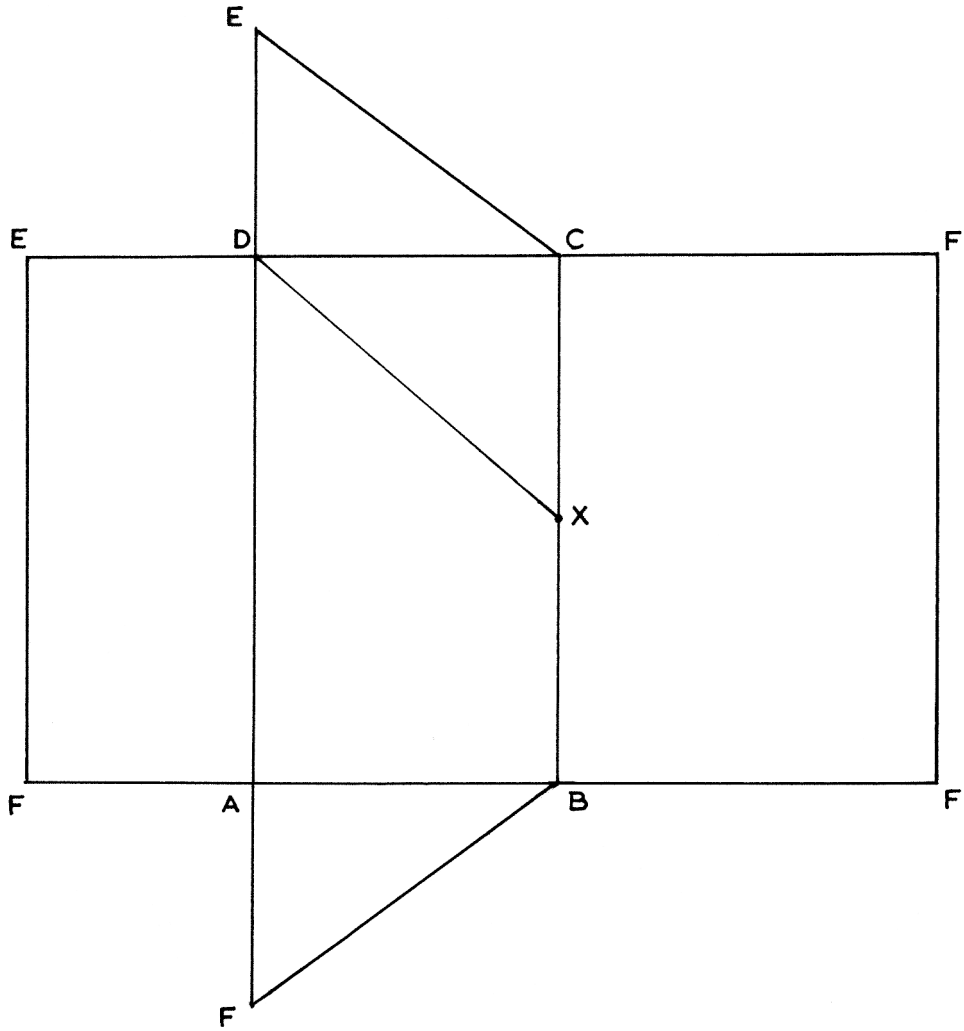


4.3 MATHEMATICS (121 AND 122)

4.3.1 Mathematics Alternative A Paper 1 (121/1)

1.	<p>Cows = 32</p> <p>Sheep = 32×12 = 384</p> <p>Goats = $384 + 1344$ = 1728</p> <p>Number of goats that remained = $\frac{1}{4} \times 1728$ = 432</p>	M1	
		M1	
		M1	
		A1 4	
2.	$\frac{\sqrt{1764}}{\sqrt[3]{2744}} = \frac{\sqrt{2^2 \times 3^2 \times 7^2}}{\sqrt[3]{2^3 \times 7^3}}$ $= \frac{2 \times 3 \times 7}{2 \times 7}$ $= 3$	M1	For prime factors of both $\sqrt{\quad}$ and $\sqrt[3]{\quad}$
		M1	
		A1	
		3	
3.	<p>Volume = $\frac{1}{3} \times \frac{22}{7} \times (14)^2 \times 18$ = 3696 cm³</p> <p>Density = $\frac{4.62 \times 1000}{3696}$ = 1.25 g/cm³</p>	M1	
		M1	
		A1	
		3	

4.



$DX = 5.3 \pm 0.1$

B1	✓ measurements and angles
B1	✓ complete net (labelled)
B1	
3	

5.

C.P. for carpet

$$= \frac{36000 \times 100}{120}$$

$$= 30000$$

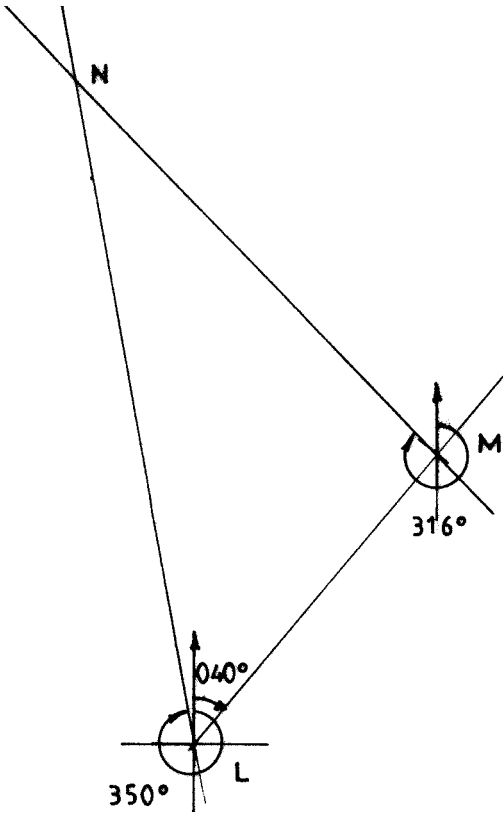
% profit made during trade fair

$$= \frac{33600 - 30000}{30000} \times 100$$

$$= 12\%$$

M1
M1
A1
3

6.	$= \frac{243^{\frac{-2}{5}} \times 125^{\frac{2}{3}}}{9^{\frac{-3}{2}}}$ $= \frac{27 \times 25}{9}$ $= 75$	M1 M1 A1 3	✓ manipulation of all indices or equivalent simplification
7.	$= \frac{\theta}{2\pi} \times \pi \times 2.1 \times 2.1 = 2.31$ $\theta = \frac{2.31 \times 2}{2.1 \times 2.1}$ $= 1.05^\circ$	M1 A1 2	
8.	$(x + 2y)^2 - (2y - 3)^2$ $= (x^2 + 4xy + 4y^2) - (4y^2 - 12y + 9)$ $= x^2 + 4xy + 12y - 9$	M1 A1 2	

<p>9.</p>	 <p>Distance $MN = 6.8 \times 100$ $= 680$ km</p>	<p>B1 B1</p>	<p>✓ location of M ✓ location of N</p>
<p>10.</p>	$(2n - 4) \times 90 = 1800$ $180n = 2160$ $n = 12$ <p>size of each exterior angle</p> $= \frac{360}{12} = 30^\circ$	<p>M1 M1 A1</p>	<p>MN = 6.8 ± 0.1 cm</p>
<p>11.</p>	<p>let age of cow be x years</p> $\therefore x\left(x - 4\frac{2}{3}\right) = 8$ $3x^2 - 14x - 24 = 0$ $(3x + 4)(x - 6) = 0$ $x = 6 \text{ or } -\frac{4}{3}$ <p>Age of cow = 6 years Age of heifer = $1\frac{1}{3}$ years</p>	<p>M1 M1 A1 B1</p>	<p>4</p>

12.	$4 \leq 3x - 2 < 9 + x$ $4 \leq 3x - 2 \quad 3x - 2 < 9 + x$ $6 \leq 3x \quad 2x < 11$ $x \geq 2 \quad x < 5\frac{1}{2}$ $\therefore 2 \leq x < 5\frac{1}{2}$ <p>Integral values 2, 3, 4, 5</p>	<p>M1</p> <p>A1</p> <p>B1</p> <p>3</p>	
13.	<p>Volume of water in container</p> $= \frac{80}{100} \times 90(40 \times 25 - \pi \times 7.5^2)$ $= 59276.54975$ $\frac{59276.54975}{1000}$ $= 59.3$	<p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>3</p>	<p>for $\frac{80}{100} \times 90$</p> <p>difference in volumes</p> <p>conversion into litres</p>
14.	<p>Angle for major arc = $360 - 105$ = 255°</p> <p>Length of arc = $\frac{255}{360} \times 2 \times 8.4 \times \frac{22}{7}$</p> $= 37.4 \text{ cm}$	<p>B1</p> <p>M1</p> <p>A1</p> <p>3</p>	
15.	<p>Amount of work = $25 \times 16 \times 9$</p> <p>Machines required</p> $= \frac{25 \times 16 \times 9}{12 \times 10}$ $= 30$	<p>M1</p> <p>M1</p> <p>A1</p> <p>3</p>	<p>÷ by 12×10</p>
16.	$ AB = \sqrt{(-3 + 2)^2 + (7 - 2)^2} = \sqrt{26}$ $ A'B' = \sqrt{4^2 + (-20)^2} = \sqrt{416}$ <p>Scale factor = $\frac{ A'B' }{ AB } = \frac{\sqrt{416}}{\sqrt{26}}$</p> $= 4$	<p>M1</p> <p>M1</p> <p>A1</p> <p>3</p>	<p>for AB and $A'B'$</p>

17.	<p>(a) Equation of L</p> $\text{gradient} = \frac{6-3}{-1-2}$ $= 3$ $\text{equation} = \frac{y-6}{x+1} = 3$ $\Rightarrow y - 3x = 9$ <p>(b) equation of P</p> $= \frac{y-6}{x+1} = -\frac{1}{3}$ $3y + x = 17$ <p>(c) equation of Q</p> $= \frac{y-2}{x-1} = 3$ $y = 3x - 1$ <p><i>x</i> intercept when $y = 0 \Rightarrow x = \frac{1}{3}$</p> <p><i>y</i> intercept when $x = 0 \Rightarrow y = -1$</p> <p>(d) Intersection of lines P and Q</p> $3y + x = 17 \dots (i)$ $y - 3x = -1 \dots (ii)$ $3y + x = 17$ $3y - 9x = -3$ $10x = 20 \Rightarrow x = 2$ <p>subset $3y + 2 = 17 \Rightarrow y = 5$</p> $\therefore \text{point of intersection } (2, 5)$	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>10</p>	<p>for both $x = 2$ and $y = 5$</p>
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18.

(a)

Class	3-5	6-8	9-11	12-14	15-17	18-20
Frequency	3	8	13	10	4	2

B1

B1

(b) (i) mean length = $\frac{\sum fx}{\sum f}$

$$= \frac{4 \times 3 + 7 \times 8 + 10 \times 13 + 13 \times 10 + 16 \times 4 + 19 \times 2}{40}$$

$$= 10.75$$

(ii)

$$= \frac{23}{40} \times 100$$

$$= 57.5\%$$

B1

M1

A1

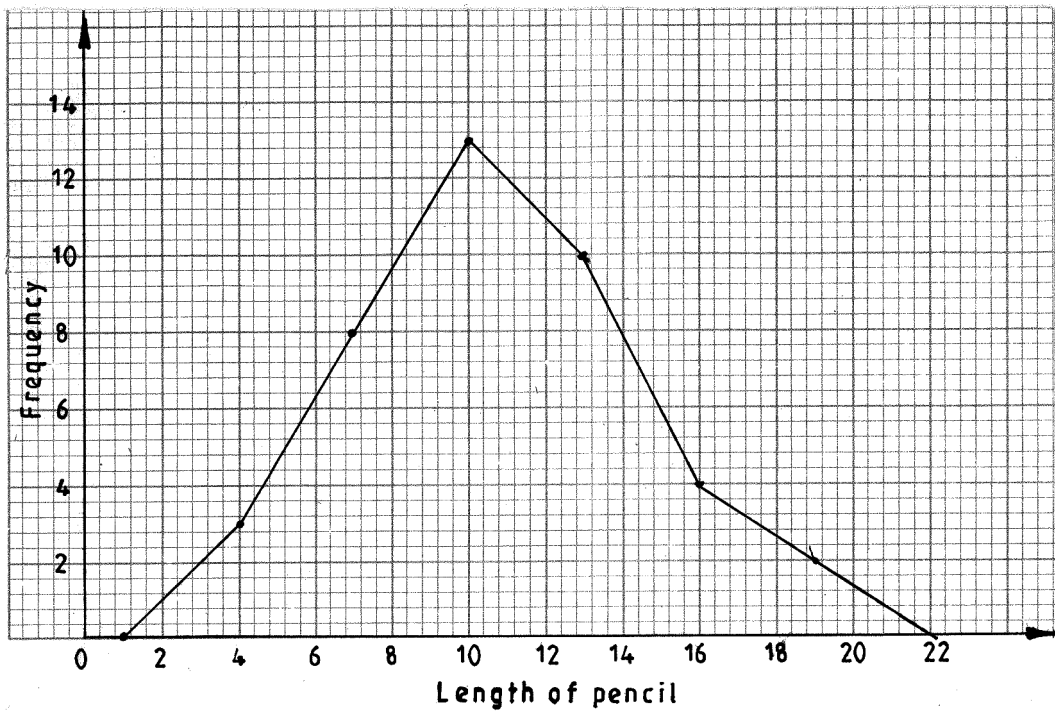
for all $\sqrt{\quad}$ mid points - i.e 4, 7, 10, 13, 16, and 19

B1

for 23

B1

(c)



S1

P1

C1

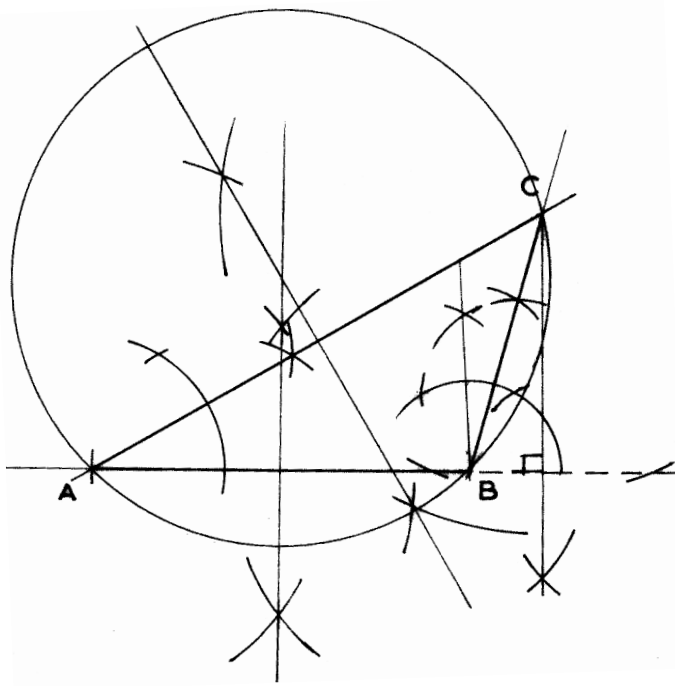
10

19.	(a)	15 m/s	B1		
	(b)	maximum speed			
		$\frac{1}{2}(15 + h) \times 10 + \frac{1}{2}(10 + 30)h = 825$	M1		
		$75 + 5h + 20h = 825$	M1		
		$25h = 750$			
		$h = 30 \text{ m/s}$	A1		
	(c)	(i)	$= \frac{30 - 15}{10}$		M1
			$= 1.5 \text{ m/s}^2$		A1
		(ii)	$= \frac{0 - 30}{20} = -1.5 \text{ m/s}^2$		B1
	(d)	$\left[\frac{1}{2}(15 + 30) \times 10 + 10 \times 30 \right] \div 20$	M1		for distance covered in first 20 seconds
	$= (225 + 300) \div 20$	M1			
	$= 26.25 \text{ m/s}$	B1			
		10			

20.	(a) base area $= \frac{1}{2} \times 15 \times 15 \sin 72 \times 5$ $= 534.97$	B1 M1 A1	use of 72°
	(b) Length AV $= \sqrt{36^2 + 15^2} = 39$	B1	
	(c) Area of triangular faces: $\frac{AB}{\sin 72} = \frac{15}{\sin 54}$ $AB = \frac{15 \sin 72}{\sin 54}$ $= 17.63$ $\therefore \text{area}$ $= \sqrt{\left\{ \frac{1}{2} (39 + 39 + 17.63)(30.185)(8.815^2) \right\}}$ $= 334.89$	M1 M1 A1	√ application of Herons formula
	Total area = $334.89 \times 5 + 534.97$ $= 2209.42$	M1	
	(d) volume of pyramid $= \frac{1}{3} \times 534.97 \times 36$ $= 6419.63 \text{ cm}^2$ $\simeq 6420 \text{ (4 s.f.)}$	A1 10	

21.	(a)	<table border="1"> <tr> <td>x</td><td>-2</td><td>-1</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td> </tr> <tr> <td>y</td><td>16</td><td>10</td><td>6</td><td>4</td><td>4</td><td>6</td><td>10</td><td>16</td><td>24</td><td>34</td><td>46</td> </tr> </table>	x	-2	-1	0	1	2	3	4	5	6	7	8	y	16	10	6	4	4	6	10	16	24	34	46		
		x	-2	-1	0	1	2	3	4	5	6	7	8															
y	16	10	6	4	4	6	10	16	24	34	46																	
									B2	y values (B1 for at least 6 correct)																		
	(b)	Area using trapezium rule							M1																			
		$= \frac{1}{2} \times 1 [16 + 46 + 2(10 + 6 + 4 + 4 + 6 + 10 + 16 + 24 + 34)]$							M1	simplification																		
		$= \frac{1}{2} [62 + 2(114)]$							A1																			
		$= 145$																										
	(c)	Area using mid-ordinate rule																										
		$= 2 \times (10 + 4 + 6 + 16 + 34)$							M1																			
		$= 140$							A1																			
	(d)	Area using integration method																										
		$\int_{-2}^8 (x^2 - 3x + 6) dx = \frac{x^3}{3} - \frac{3x^2}{2} + 6x \Big _{-2}^8$							M1	✓ integration																		
		$= \left[\frac{512}{3} - \frac{192}{2} + 48 \right] - \left[\frac{-8}{3} - \frac{3 \times 4}{2} - 12 \right]$							M1																			
		$= 122 \frac{2}{3} + 20 \frac{2}{3}$							A1																			
		$= 143 \frac{1}{3}$							10																			

22. (a) (i)



(ii)

$$\text{radius} = 3.5 \pm 0.1$$

(iii) height construction
height = 3.4 ± 0.1

(b) area of circle outside triangle
 $= \pi \times 3.5^2 - \frac{1}{2} \times 3.4 \times 5$
 $\simeq 29.98$

B1 construction of 30°
 B1 construction of 105°
 B1 completion of $\triangle ABC$

B1 \perp bisectors

B1 circle

B1

B1 height constructed
 B1

M1

A1

10

23.	(a)	$\tan \theta = \frac{70}{240}$	M1
		$= 0.2917$	
		$\theta = 16.26^\circ$	A1
	(b)	$AC = \sqrt{70^2 + 240^2}$	
		$= 250 \text{ m}$	B1
		$\angle ACD = 150^\circ - (90^\circ - 16.26^\circ)$	M1
		$= 76.26^\circ$	
		$AD^2 = 200^2 + 250^2 - 2 \times 200 \times 250 \cos 76.26$	M1
		$AD = \sqrt{40000 + 62500 - 100000 \cos 76.26^\circ}$	A1
		$= 280.6$	
(c)	Area of plot		
	$= \frac{1}{2} \times 240 \times 70 + \frac{1}{2} \times 250 \times 200 \sin 76.26^\circ$	M1	
	$= 8400 + 24284.59$	M1	
	$= 32684.59 \text{ m}^2$		
	$= \frac{32684.59}{10000}$	M1	
	$= 3.27 \text{ ha}$	A1	
		10	

24.	<p>(a) Value of y when $x = -1$ $y = -1 - 4 + 3 = -2$</p> <p>(b) Stationary points $\frac{dy}{dx} = 3x^2 - 8x - 3$</p> <p>for stationary points $3x^2 - 8x - 3 = 0$ $(3x + 1)(x - 3) = 0$ $x = -\frac{1}{3}$ or $x = 3$ when $x = -\frac{1}{3}$, $y = \frac{14}{27}$ when $x = 3$, $y = -18$ \therefore stationary points $\left(-\frac{1}{3}, \frac{14}{27}\right)$ and $(3, -18)$</p> <p>(c) Equation of normal to curve: gradient of tangent at $x = 1$</p> $\frac{dy}{dx} = 3 - 8 - 3 = -8$ <p>gradient of normal $= \frac{1}{8}$</p> <p>\therefore equation of normal at $x = 1$ $\frac{y + 6}{x - 1} = \frac{1}{8}$</p> $y + 6 = \frac{1}{8}x - \frac{1}{8}$ $y = \frac{1}{8}x - 6\frac{1}{8}$	<p>B1</p> <p>M1</p> <p>M1 A1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p>	
		10	

4.3.2 Mathematics Alternative A Paper 2 (121/2)

1.	Limits: 12.5 ± 0.05 m and 9.23 ± 0.005 m Maximum difference $= 12.55 - 9.225$ $= 3.325$ m	B1																			
		M1 A1 3																			
2.	a) First 6 terms -7, -4, -1, 2, 5, 8 b) Sum of 1 st 50 terms $S_{50} = \frac{50}{2}\{2 \times -7 + 49 \times 3\}$ $= 3325$	B1																			
		M1 A1 3																			
		3																			
3.	a) $\angle BAC = 70^\circ - 30^\circ = 40^\circ$ Reflex $\angle BOC = 360^\circ - 80^\circ$ $= 280^\circ$ b) $\angle ACO = 40^\circ - 30^\circ = 10^\circ$	B1																			
		B1 B1 3																			
		3																			
4.	$L = \frac{kM}{N^2}$ $2 = \frac{k \times 12}{36}$ $k = 6$ \therefore equation $L = \frac{6M}{N^2}$	B1																			
		M1 A1 3																			
		3																			
5.	<table border="1"> <thead> <tr> <th>Marks</th> <th>Frequency</th> <th>c.f</th> </tr> </thead> <tbody> <tr> <td>1 - 10</td> <td>2</td> <td>2</td> </tr> <tr> <td>11 - 20</td> <td>4</td> <td>6</td> </tr> <tr> <td>21 - 30</td> <td>11</td> <td>17</td> </tr> <tr> <td>31 - 40</td> <td>5</td> <td>22</td> </tr> <tr> <td>41 - 50</td> <td>3</td> <td>25</td> </tr> </tbody> </table>	Marks	Frequency	c.f	1 - 10	2	2	11 - 20	4	6	21 - 30	11	17	31 - 40	5	22	41 - 50	3	25	B1 for c.f	
	Marks	Frequency	c.f																		
	1 - 10	2	2																		
	11 - 20	4	6																		
	21 - 30	11	17																		
31 - 40	5	22																			
41 - 50	3	25																			
Median																					
$= 20.5 + \frac{12.5 - 6}{11} \times 10$																					
$= 20.5 + 5.91$																					
$= 26.41$																					
$\simeq 26$																					
	M1 M1 A1 4																				

6.	Amplitude = 2 Period = $\frac{360}{3} = 120^\circ$	B1 B1 <hr/> 2	
7.	Area scale factor = $\frac{30}{5} = 6$ $4x - 2x + 2 = 6$ $2x = 4$ $x = 2$	B1 M1 A1 <hr/> 3	
8.	$(3 - x)^7 = 3^7 - 7(3)^6x + 21(3)^5x^2 - 35(3)^4x^3$ $+ 35(3)^3x^4 + \dots$ $= 2187 - 5103x + 5103x^2 - 2835x^3 + 945x^4$ $(2.8)^7 = (3 - 0.2)^7$ $= 2187 - 5103(0.2) + 5103(0.2)^2$ $- 2835(0.2)^3 + 945(0.2)^4$ $= 1349.352$	B1 M1 A1 <hr/> 3	
9.	$\text{Log} \frac{15^2}{x} = \log 5(x - 4)$ $\frac{15^2}{x} = 5(x - 4)$ $x^2 - 4x - 45 = 0$ $(x - 9)(x + 5) = 0$ $x = 9 \text{ or } -5$ $x = 9$	M1 M1 M1 A1 <hr/> 4	
10.	$PR = \sqrt{60^2 + 11^2} = 61$ $\text{Tan } \theta = \frac{10}{61}$ $\theta = 9.31^\circ$	B1 M1 A1 <hr/> 3	

11.	$3x - y = 9 \quad \dots \times x$ $x^2 - xy = 4$ $3x^2 - xy = 9x$ $\frac{x^2 - xy = 4}{2x^2} = 9x - 4$ $2x^2 - 9x + 4 = 0$ $(2x - 1)(x - 4) = 0$ $x = \frac{1}{2} \quad \text{or} \quad x = 4$ $y = 3\left(\frac{1}{2}\right) - 9 \quad \text{or} \quad 3(4) - 9$ $= -7\frac{1}{2} \quad \text{or} \quad 3$	M1 M1 A1 B1 4	Attempt to solve Factors
12.	$\left(1 + \frac{r}{100}\right)^4 = \frac{495000}{280000}$ $1 + \frac{r}{100} = 1.153$ $r = 15.3$	M1 M1 A1 3	
13.	$8008 = \frac{40 + \theta}{360} \times 2 \times \frac{22}{7} \times 6370$ $40 + \theta = \frac{8008 \times 360 \times 7}{2 \times 22 \times 6370} = 72$ $\theta = 72^\circ - 40^\circ$ $= 32^\circ$ <p>Position of B(32° S, 20°W)</p>	M1 M1 A1 3	or 32° seen
14.	$\underline{r} + \underline{s} = (7\underline{i} + 2\underline{j} - \underline{k}) + (-\underline{i} + \underline{j} - \underline{k})$ $= 6\underline{i} + 3\underline{j} - 2\underline{k}$ $ \underline{r} + \underline{s} = \sqrt{6^2 + 3^2 + (-2)^2}$ $= 7$	B1 M1 A1 3	

15.	$y = \int (x^2 - 4x + 3) dx$ $= \frac{1}{3}x^3 - 2x^2 + 3x + c$ $0 = \frac{1}{3} - 2 + 3 + c$ $\therefore c = -\frac{4}{3}$ $\therefore y = \frac{1}{3}x^3 - 2x^2 + 3x - \frac{4}{3}$	M1 M1 A1	
		3	
16.	<p>Temperature at the 2nd minute = 60° Temperature at the 11th minute = 18°</p> <p>Average rate of cooling</p> $= \frac{60 - 18}{2 - 11}$ $= \frac{42}{ 9 }$ $= 4\frac{2}{3} \text{ C/min}$	B1 M1 A1	for both ✓
		3	
17.	<p>a) $A = \frac{3}{4}B, C = 2B$ $\Rightarrow A:B:C = \frac{3}{4}B:B:2B$ $= 3:4:8$</p> <p>b) $\left(\frac{168}{8} \times 4\right)$ litres $= 84 \text{ l}$</p> <p>c) (i) $\frac{3 \times 160 + 4 \times 205 + 8 \times 100}{3 + 4 + 8}$ $= \text{Ksh } 140$</p> <p>(ii) $\frac{182 - 140}{140} \times 100\%$ $= 30\%$</p> <p>(iii) $\text{Ksh } 140 \times \frac{125}{100}$ $= \text{Ksh } 175$</p>	M1 A1 M1 A1 M1 A1 M1 A1	
		10	

18.	<p>a) (i) $(50 + 40)(50) = 30(30 + x)$ $4500 = 900 + 30x$ $30x = 3600$ $QS = x = 120 \text{ cm}$</p> <p>(ii) $RS = \frac{1}{2}QS$ $= \frac{1}{2}(120) = 60 \text{ cm}$ $OR = \sqrt{61^2 - 60^2}$ $= 11 \text{ cm}$</p> <p>b) (i) $\sin \theta = \frac{60}{61}$ $\theta = 79.6^\circ$</p> <p>(ii) Angle at the centre $= 2 \times 79.6$ $= 159.2^\circ$</p> <p>Length of minor arc QS $= \frac{159.2}{360} \times 2\pi \times 61$ $= 169.5 \text{ cm}$</p>	<p>M1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>10</p>	<p>or equivalent</p>
19.	<p>a) (i) $38392 + 2108$ $= \text{Ksh } 41000$</p> <p>(ii) $10164 \times 0.1 + 9576 \times 0.15 + 9576 \times 0.2$ $+ 9576 \times 0.25 + 2108 \times 0.3$ $= 1016.4 + 1436.4 + 1915.2 + 2394 + 632.4$ $= \text{Ksh } 7394.4$</p> <p>monthly income tax $= 7394.4 - 1162$ $= \text{Ksh } 6232.4$</p> <p>b) Amount saved in coop society $= \frac{5}{100} \times (41000 - 15000)$ $= \text{Ksh } 1300$</p> <p>Nett pay $41000 - (6232.4 + 1300)$ $= \text{Ksh } 33467.6$</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>10</p>	<p>$\sqrt{1^{\text{st}}}$ band</p> <p>$\sqrt{3}$ middle bands</p> <p>$\sqrt{\text{last } (5^{\text{th}})}$ band</p>

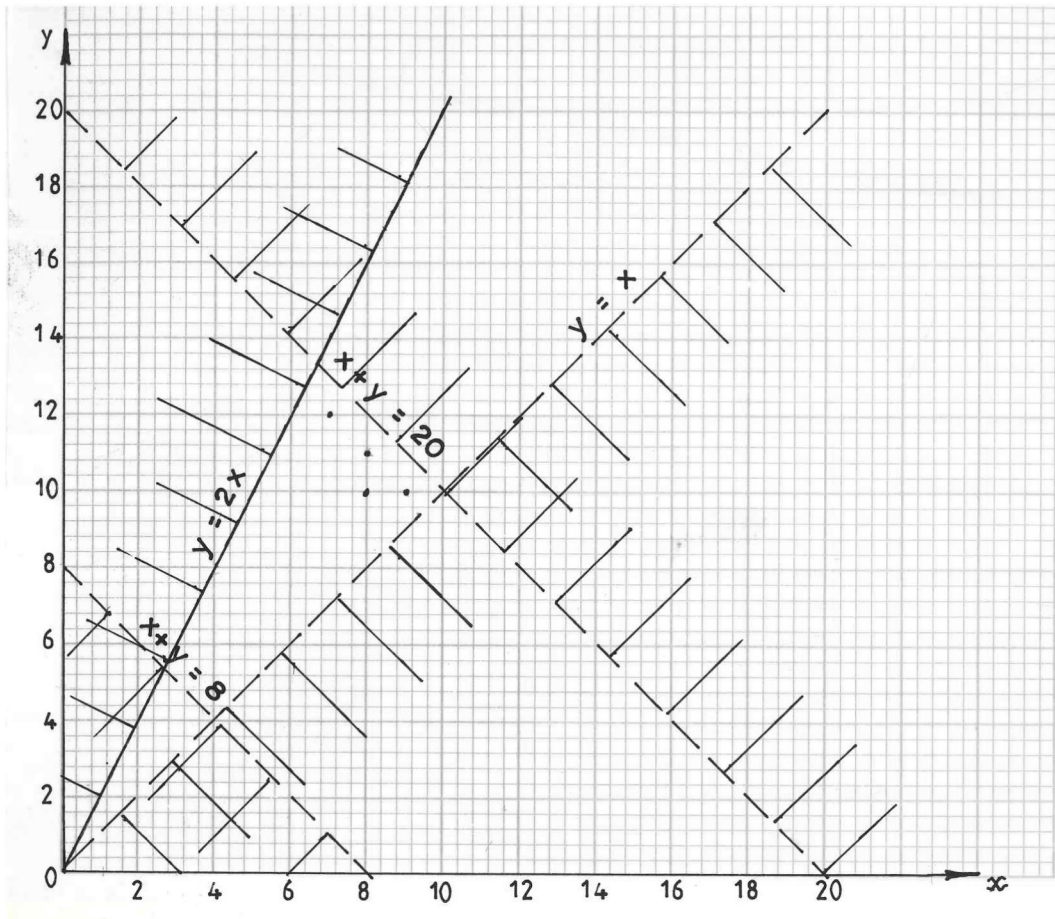
20. a) $y > x$
 $y \leq 2x$

$x + y < 20$
 $x + y > 8$

B1
 B1

B1
 B1

b) (i)



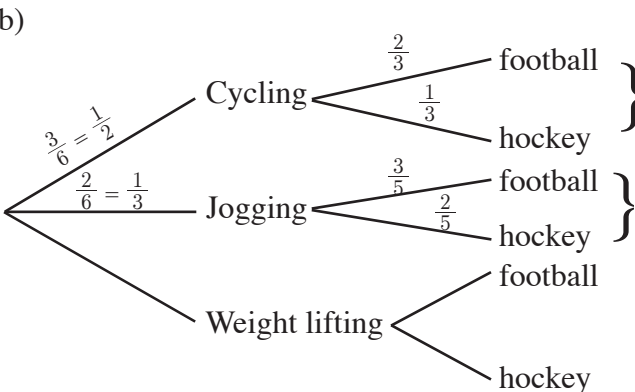
(ii) Maximum area:

$$9 \times 10 = 90 \text{ m}^2$$

B1 line $y = 2x$ and $\sqrt{\quad}$ shading
 B1 broken line $x + y = 20$ and $\sqrt{\quad}$ shading
 B1 broken line $x + y = 8$ and $\sqrt{\quad}$ shading
 B1 broken line $y = x$ and $\sqrt{\quad}$ shading

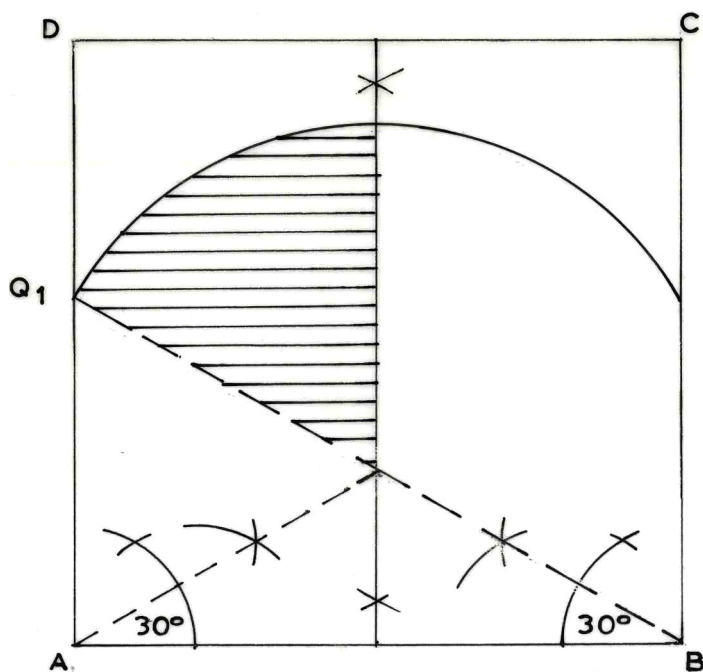
M1
 A1

10

21.	<p>a) (i) $\frac{3}{6} + \frac{1}{6}$</p> <p style="padding-left: 40px;">$= \frac{2}{3}$</p> <p>(ii) $\frac{2}{6} \times \frac{2}{6}$</p> <p style="padding-left: 40px;">$= \frac{1}{9}$</p> <p>b)</p>  <p>c) (i) P(Gataro plays football)</p> <p style="padding-left: 40px;">$= \frac{1}{2} \times \frac{2}{3} + \frac{1}{3} \times \frac{3}{5} + \frac{1}{6} \times \frac{1}{2}$</p> <p style="padding-left: 40px;">$= \frac{37}{60}$</p> <p>(ii) P(neither jogs nor plays football)</p> <p style="padding-left: 40px;">$= \frac{1}{2} \times \frac{1}{3} + \frac{1}{6} \times \frac{1}{2}$</p> <p style="padding-left: 40px;">$= \frac{1}{4}$</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p>	
		10	

22.	<p>a) (i) $\underline{BA} = \underline{a} - \underline{b}$</p> <p>(ii) $\underline{BN} = \frac{1}{3}\underline{BA} = \frac{1}{3}(\underline{a} - \underline{b})$</p> <p>(iii) $\underline{ON} = \underline{b} + \frac{1}{3}(\underline{a} - \underline{b})$ $= \frac{1}{3}\underline{a} + \frac{2}{3}\underline{b}$</p> <p>b) $\underline{BX} = h\underline{BM} = h\left(\frac{1}{2}\underline{a} - \underline{b}\right)$ $\underline{OX} = k\underline{ON} = k\left(\frac{1}{3}\underline{a} + \frac{2}{3}\underline{b}\right)$ also $\underline{OX} = \underline{OB} + \underline{BX}$ $= \underline{b} + h\left(\frac{1}{2}\underline{a} - \underline{b}\right)$</p> <p>$k\left(\frac{1}{3}\underline{a} + \frac{2}{3}\underline{b}\right) = \underline{b} + h\left(\frac{1}{2}\underline{a} - \underline{b}\right)$ $\frac{1}{3}k\underline{a} = \frac{1}{2}h\underline{a}$ $\frac{1}{3}k = \frac{1}{2}h \implies k = \frac{3}{2}h \dots\dots\dots (i)$ $\frac{2}{3}k\underline{b} = \underline{b} - h\underline{b}$ $\frac{2}{3}k = 1 - h \dots\dots\dots (ii)$</p> <p>Substituting $k = \frac{3}{2}h$ in (ii)</p> <p>$\frac{2}{3}\left(\frac{3}{2}h\right) = 1 - h \implies h = \frac{1}{2}$</p> <p>Substituting $h = \frac{1}{2}$ in (i)</p> <p>$k = \frac{3}{2}\left(\frac{1}{2}\right) = \frac{3}{4}$</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>10</p>	<p>for $h = \frac{1}{2}$ and $k = \frac{3}{4}$</p>
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23.



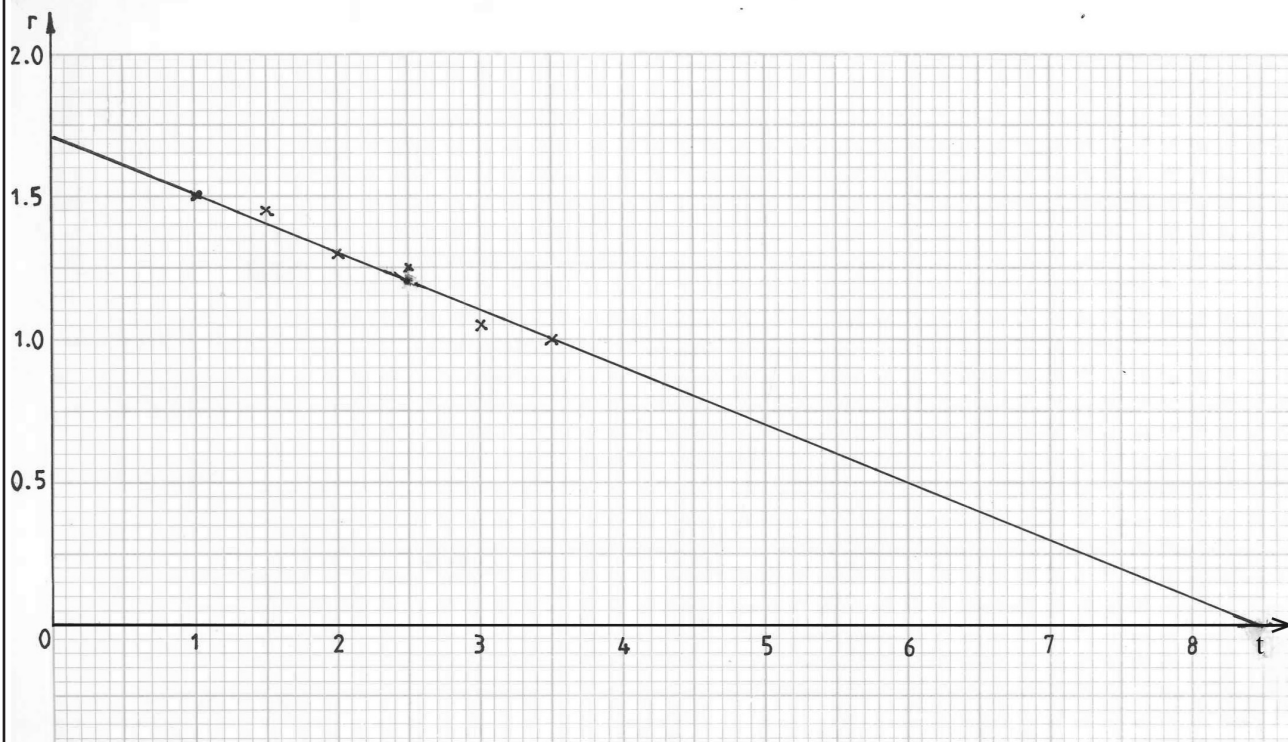
- (i)
- (ii)

b) (i) $9.2 \times 10 = 92 \text{ m}$

(ii) area of region bounded by locus of P,
 locus of Q and line BQ₁
 angle = 60° radius = 46 m
 $= \pi \times 46^2 \times \frac{60}{360}$
 $= 1107.94$
 $\approx 1108 \text{ m}^2$

B2	locus of P
B1	construction of 30°
B1	identification of centre
B1	drawing of arc
B1	
B1	Identifying region
B1	for radius and angle of sector
M1	
A1	
10	

24. a)



b) (i) value of a

$$= \frac{-0.7}{3.5}$$

$$= -0.2$$
 value of k = 1.7

(ii) equation: $r = -0.2t + 1.7$

(iii) value of t when $r = 0$
 $\therefore 0 = -0.2t + 1.7$
 $0.2t = 1.7$

$$t = \frac{1.7}{0.2} = 8.5$$

S1 \checkmark scale
 P2 (P1 for 4 points \checkmark plotted)
 L1 \checkmark line
 M1

A1
 B1

B1

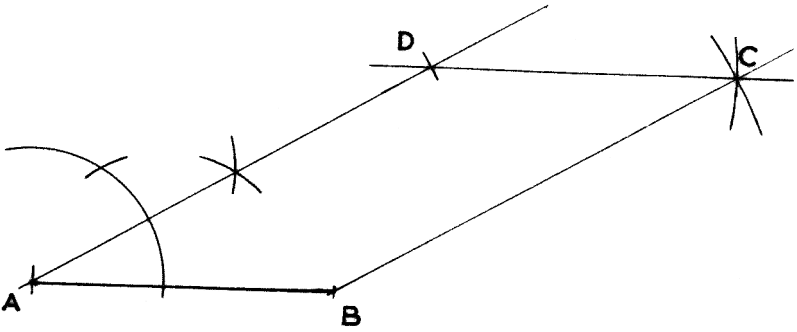
M1

A1

10

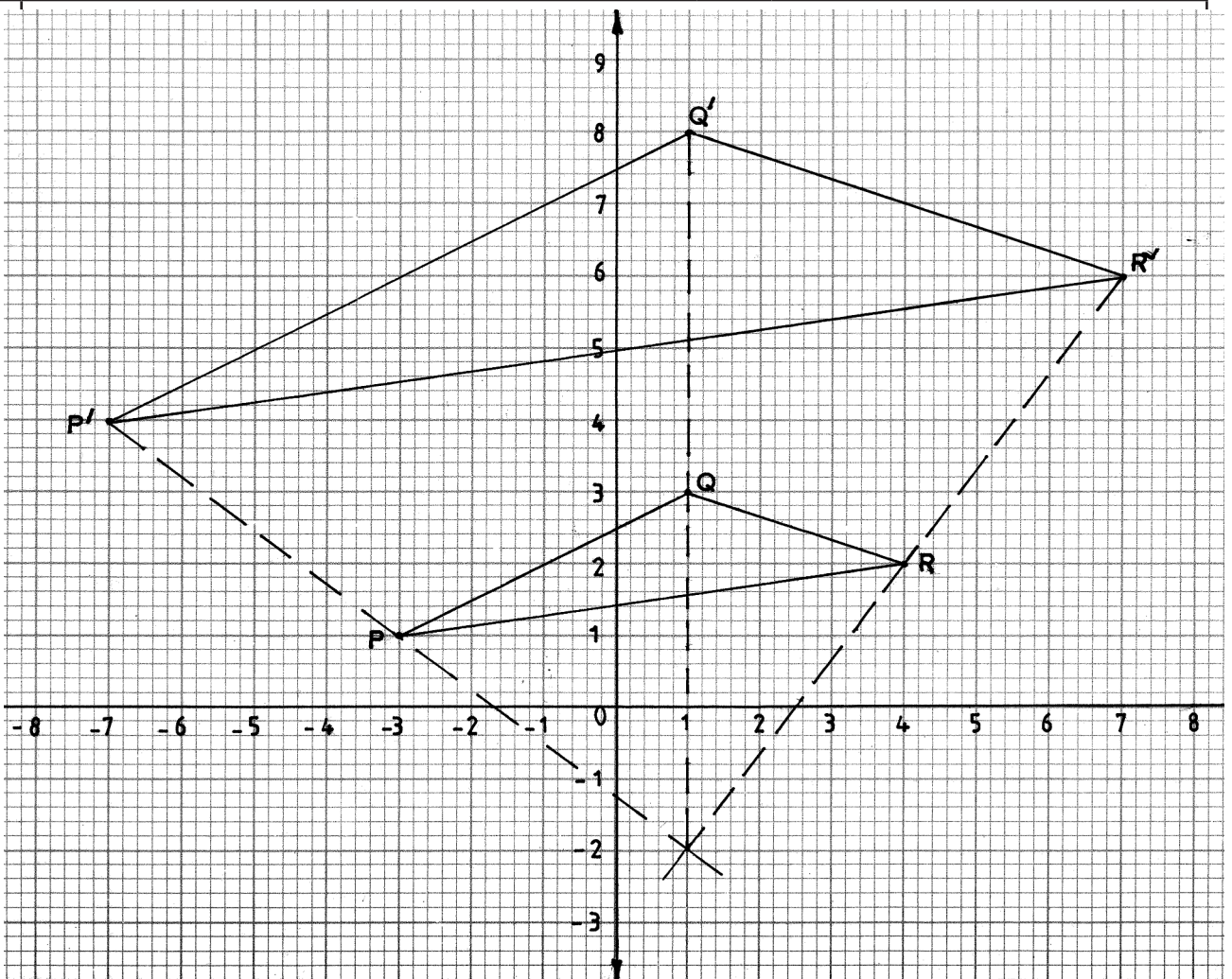
4.3.3 Mathematics Alternative B (122/1)

1.	$\frac{-8 \times +2 + -11}{+18 \div -2 \times +3} = \frac{-27}{-27}$ $= 1$	M1 A1 2	
2.	Number of boys = $630 - 84$ $= 546$ Number of students = $630 + 546$ $= 1176$ Number of parents = $1176 \div 4$ $= 294$	M1 M1 A1 3	
3.	$3(78 - y) + 5y = 300$ $2y = 66$ $y = 33$ $\therefore x = 78 - 48 = 45$ $10x + 15y = 450 + 495 = 945$	M1 A1 B1 3	
4.	(a) $96 = 2^5 \times 3$ $84 = 2^2 \times 3 \times 7$ $36 = 2^2 \times 3^2$ GCD of 96, 84 and 36 = $2^2 \times 3 = 12$ (b) Number of packets of foodstuffs $= \frac{96}{12} + \frac{84}{12} + \frac{36}{12}$ $= 8 + 7 + 3 = 18$	M1 A1 M1 A1 4	or equivalent
5.	$\frac{128}{2^5 \div 2^8} = \frac{2^7}{2^{-3}}$ $= 2^{10}$	B1 B1 B1 3	$\sqrt{\text{numerator}}$ $\sqrt{\text{denominator}}$

6.		<table border="1"> <tbody> <tr> <td>B1</td> <td>✓ construction of 30°</td> </tr> <tr> <td>B1</td> <td>✓ construction of AD = 6 cm</td> </tr> <tr> <td>B1</td> <td>identifying C and completing parallelogram</td> </tr> <tr> <td>3</td> <td></td> </tr> </tbody> </table>	B1	✓ construction of 30°	B1	✓ construction of AD = 6 cm	B1	identifying C and completing parallelogram	3	
B1	✓ construction of 30°									
B1	✓ construction of AD = 6 cm									
B1	identifying C and completing parallelogram									
3										
7.	$4\alpha + \alpha + 10 = 90^\circ$ $5\alpha = 80^\circ$ $\alpha = 16^\circ$ $\sin \alpha = 0.276$	<table border="1"> <tbody> <tr> <td>M1</td> <td></td> </tr> <tr> <td>A1</td> <td></td> </tr> <tr> <td>B1</td> <td></td> </tr> <tr> <td>3</td> <td></td> </tr> </tbody> </table>	M1		A1		B1		3	
M1										
A1										
B1										
3										
8.	$\frac{0.375 \div 0.06 - 4.2}{3.96 + 2.8 \times 0.05} = \frac{6.25 - 4.2}{3.96 + 0.14}$ $= \frac{2.05}{4.1}$ $= 0.5$	<table border="1"> <tbody> <tr> <td>M1</td> <td>Evidence of division and multiplication should be seen.</td> </tr> <tr> <td>M1</td> <td></td> </tr> <tr> <td>A1</td> <td></td> </tr> <tr> <td>3</td> <td></td> </tr> </tbody> </table>	M1	Evidence of division and multiplication should be seen.	M1		A1		3	
M1	Evidence of division and multiplication should be seen.									
M1										
A1										
3										
9.	<p>Mangoes: $2x + x + \frac{1}{3}x$</p> $= 3\frac{1}{3}x$ <p>Oranges: $\frac{1}{3}y + y + \frac{2}{3}y = 2y$</p> <p>Total Fruits = $3\frac{1}{3}x + 2y$</p>	<table border="1"> <tbody> <tr> <td>M1</td> <td></td> </tr> <tr> <td>M1</td> <td></td> </tr> <tr> <td>A1</td> <td></td> </tr> <tr> <td>3</td> <td></td> </tr> </tbody> </table>	M1		M1		A1		3	
M1										
M1										
A1										
3										

13.	$2x^2 + 6y - 3x - 4xy$ $= 2x^2 - 4xy - 3x + 6y$ $= 2x(x - 2y) - 3(x - 2y)$ $= (2x - 3)(x - 2y)$	M1 A1 2	or equivalent
14.	$x^2 \sin 30^\circ = 34$ $x = \sqrt{\frac{34}{\sin 30}}$ $\simeq 8 \text{ cm}$	M1 M1 A1 3	

15.



- (a) $\triangle PQR$
 $\triangle P'Q'R'$
 (b) Centre of enlargement $(1, -2)$
 Scale factor of enlargement $= \frac{10}{5} = 2$

B1
 B1
 B1
 B1

4

16. $\frac{L}{2.1} = \frac{L+5}{3.5}$

$3.5L - 2.1L = 10.5$

$L = 7.5$

$L = 5 + 7.5 = 12.5$

Curved area

$= \frac{22}{7} \times (3.5 \times 12.5 - 2.1 \times 7.5)$

$= 88 \text{ cm}^2$

M1

M1 for area
 M1 for difference

A1

4

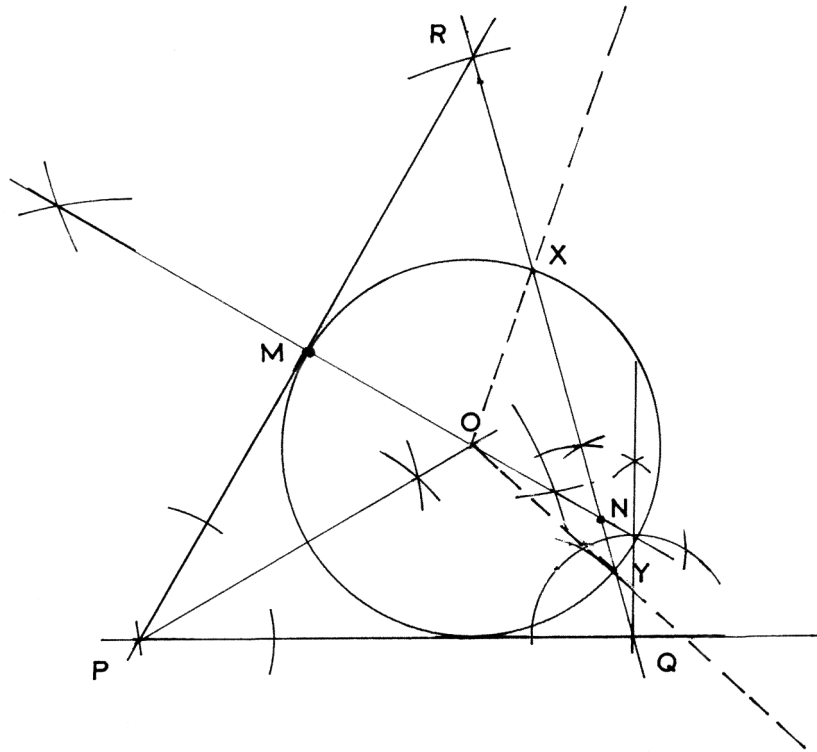
17.	(a) (i) Mumo's contribution:	$= \frac{25}{100} \times (30000 + 50000)$	M1	
		$= 20000$	A1	
	(ii) Ratio - Keya : Limo : Mumo	$= 30000:50000:20000$	M1	
		$= 3:5:2$	A1	
	(b) Mumo's share of profit	$= \frac{2}{10} \times 25000$	M1	
		$= 5000$	A1	
	(c) (i) $20000 + x = 80000 \times \frac{7}{8}$		M1	
		$x = 50000$	A1	
	(ii) Mumo's % contribution in business during 2 nd year	$= \frac{70000}{150000} \times 100$	M1	or $\frac{7}{15} \times 100\%$ M1
		$= 46\frac{2}{3}\%$	A1	$= 46\frac{2}{3}\%$ A1
			10	

18.	<p>(a) $1.54l = 1540 \text{ cm}^3$</p> <p>Volume = $\frac{22}{7} \times r^2 \times 10 = 1540$</p> $r = \sqrt{\frac{1540 \times 7}{22 \times 10}}$ $= 7$ <p>\therefore Diameter = $2 \times 7 = 14 \text{ cm}$</p> <p>(b) (i) Length of ribbon</p> $= 2 \times \frac{22}{7} \times 14 + 2 \times 2$ $= 88 + 4 = 92$ <p>(ii) Surface area covered by ribbon</p> $= 88 \times 1.5 = 132 \text{ cm}^2$ <p>(c) Surface area</p> $= \frac{22}{7} \times 49 + \frac{22}{7} \times 14 \times 10$ $= 154 + 440$ $= 594 \text{ cm}^2$	<p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>10</p>	<p>addition of the overlap</p>
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19.	(a) Scale used:		
	9 cm represent 90 m	B1	
	\therefore scale 1:1000	B1	
	(b) (i) perimeter of homestead		
	$(2 \times 10) \times 4$	M1	
	$= 80 \text{ m}$	A1	
	(ii) Area of piece of land in ha.		
	$AB = 13.8 \times 10 = 138;$ $BC = 6 \times 10 = 60$		
	$\frac{\frac{1}{2}(60 + 90) \times 138}{10000}$	M1 M1	conversion to Hectares
	$= 1.035 \text{ ha}$	A1	
(c) \perp distance from centre of homestead to side CD shown	B1		
Distance, 3.6 cm, on map	B1		
Actual distance $3.6 \times 10 = 36 \text{ m}$	B1		
	10		

20.	<p>(a) Gradient of L_1</p> $= \frac{1 - -2}{6 - -3}$ $= \frac{1}{3}$ <p>equation of L_1</p> $= \frac{y - 1}{x - 6} = \frac{1}{3}$ $3y - 3 = x - 6$ $3y = x - 3$ $y = \frac{1}{3}x - 1$ <p>(b) Gradient of L_2</p> $= \frac{-1}{\frac{1}{3}}$ $= -3$ <p>\therefore equation $\frac{y - 2}{x - -1} = -3$</p> $y = -3x - 1$ $\Rightarrow 3x + y + 1 = 0$ <p>(c) equation of L_3</p> $\frac{y - 1}{x - 1} = -3$ $y - 1 = -3(x - 1)$ $y = -3x + 4$ <p>x intercept: when $y = 0$, $x = \frac{4}{3}$ \therefore coordinates of x intercepts $\left(\frac{4}{3}, 0\right)$</p> <p>$y$ intercept: when $x = 0$, $y = 4$ \therefore coordinates of y intercept $(0, 4)$</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>B1</p> <p>B1</p> <p>10</p>	
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21.



(a) Lines PQ and PR
 angle 75° constructed
 completion of $\triangle PQR$.

B1
B1
B1
B1

(b) (i) \perp bisector of PR

 (ii) angle bisector $\angle QPR$
 $\angle POM 60^\circ \pm 1^\circ$

 (iii) circle with radius OM
 $XY = 4.3 \pm 0.1$
 $\angle XOY 114^\circ \pm 1^\circ$

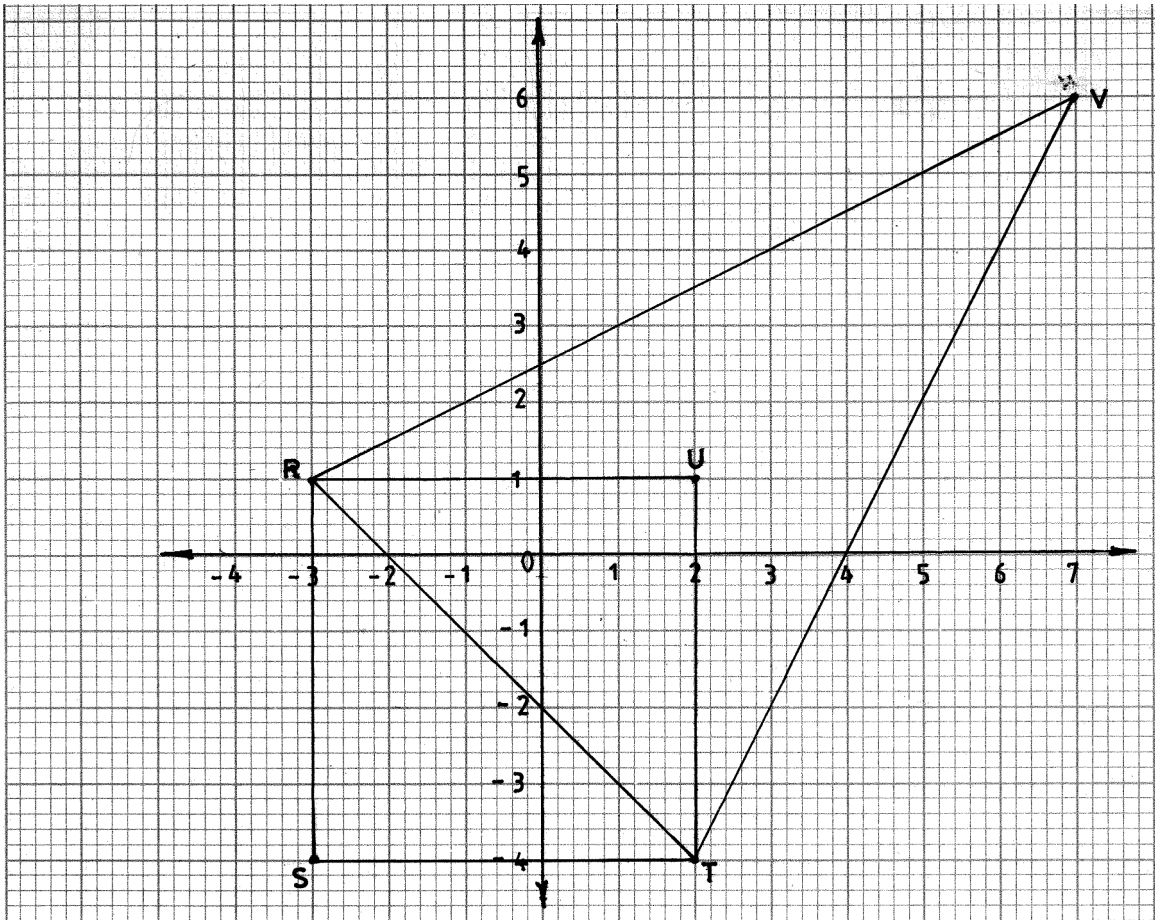
B1
B1
B1
B1
B1
B1

10

22.	(a) (i)	$\frac{400\text{m}}{64\text{s}}$	M1	
		$= 6.25 \text{ m/s}$	A1	
	(ii)	speed during second lap		
		6.25×1.06 6.625 m/s	M1 A1	
	(b) (i)	total time for two laps		
		time for 2 nd lap $= \frac{400}{6.625}$	M1	
		$\approx 60.38 \text{ s}$		
		total time $= 64 + 60.38$ $= 124.38 \text{ s}$	M1 A1	
	(ii)	average speed in km/h		
		$\frac{800}{124.38} \text{ m/s}$	M1	
$= \frac{800}{124.38} \times \frac{3600}{1000}$		M1	✓ conversion	
$= 23.15 \text{ km/h}$		A1		
			10	

23.	(a) (i)	amount of money spent		
		$= \frac{420}{8} \times 20 + 50$	M1	
		$= 1100$	A1	
	(a) (ii)	number of bananas sold		
		$= 420 + \frac{420}{70} - 14$		
		$= 412$	B1	
	(b) (i)	s.p. of bananas		
		$= 1100 \times 1.6$	M1	
		$= 1760$		
		let x be number of bananas sold at sh 30		
		$\therefore \frac{x}{5} \times 30 + \frac{412-x}{3} \times 10 = 1760$	M1	
		$18x + 412 - 10x = 1760$	M1	
$x = 145$		A1		
(ii) No of bananas sold at sh 10				
$= 412 - 145 = 267$		B1		
Amount of money obtained				
$= \frac{267}{3} \times 10$	M1			
$= 890$	A1			
		10		

24.



(a) (i) $\triangle RST$ ✓ drawn

B1

(ii) Area of $\triangle RST$: $\frac{1}{2} \times 5^2$
 $= 12.5$

M1
 A1

(b) (i) Plotting point U
 coordinates of point U (2, 1)

B1
 B1

(ii) Plotting of point V
 coordinates of point V (7, 6)

B1
 B1

(c) Area of quadrilateral RSTV
 diagonals $RT = \sqrt{50}$
 and $SV = \sqrt{200}$

B1 for RT and SV

$$\therefore \text{Area} = \frac{1}{2} \times \sqrt{50} \times \sqrt{200}$$

M1

$$= \frac{1}{2} \times 5\sqrt{2} \times 10\sqrt{2}$$

$$= 50$$

A1

10